

# MRI-driven outflows in accretion disks

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# Outline

## **I. Angular momentum transport in accretion disks**

- MHD turbulence vs. disc winds
- Numerical methods

## **II. Local outflows from turbulent discs (Fromang et al. 2013)**

- Stratified shearing boxes simulations
- Connexion with classical theory

## **III. The case of protoplanetary disks (Lesur et al. 2014)**

- B-field dissipation in PP disks
- The Hall effect: local simulations
- Including Ohmic, Hall & ambipolar: results & problems

## Origin of angular momentum transport in accretion disks?

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graph TD; A[Origin of angular momentum transport in accretion disks?] --> B[Internal source]; A --> C[External source];
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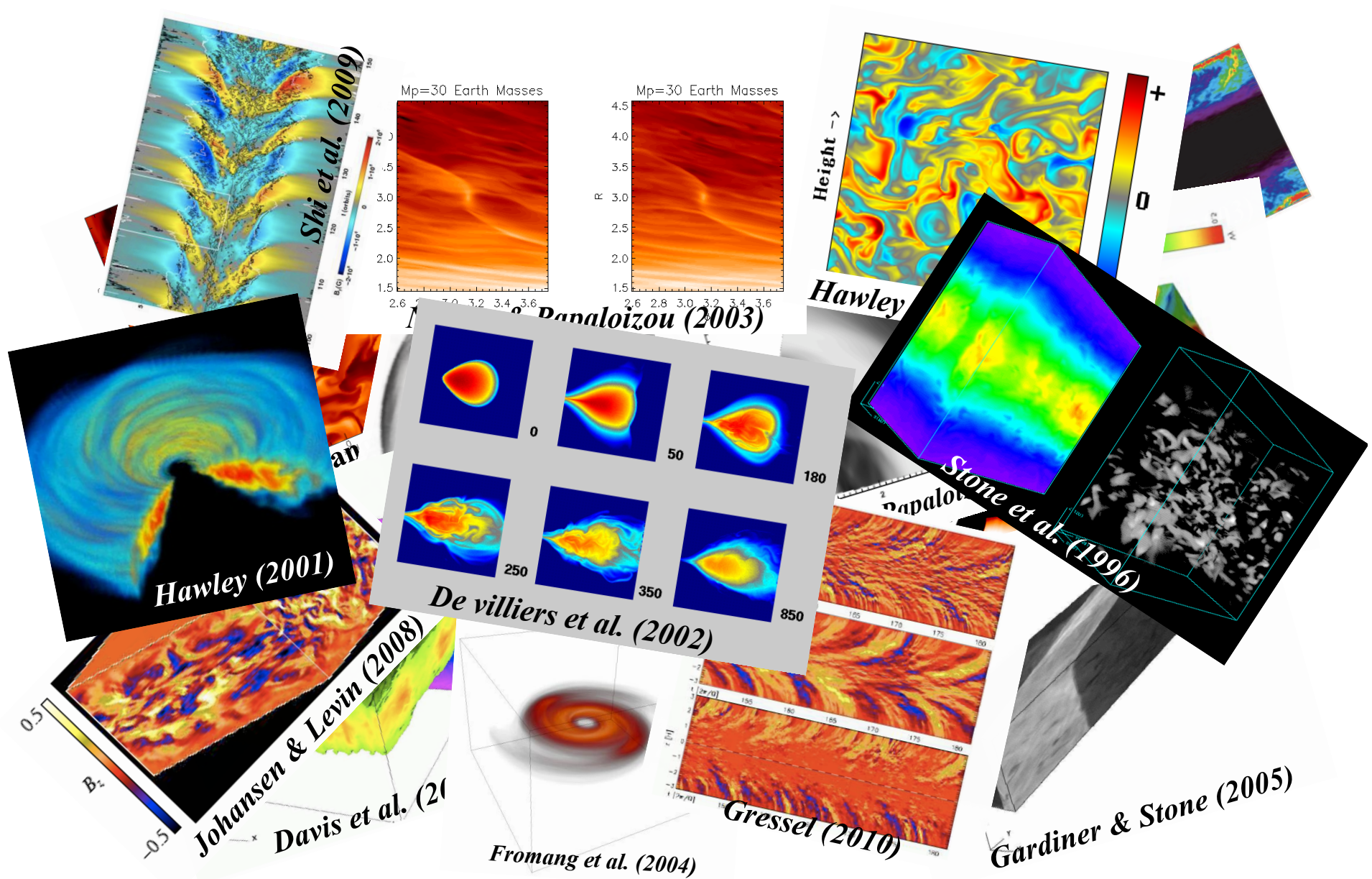
### **Internal source**

MHD turbulence driven by the magnetorotational instability  
*(Balbus & Hawley 1991)*

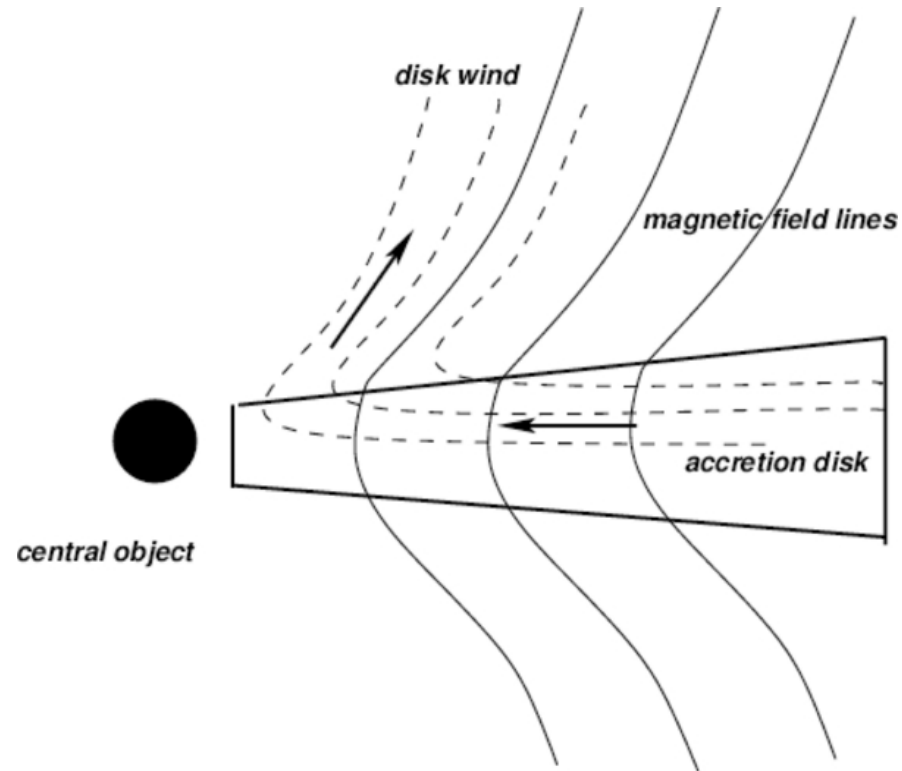
### **External source**

Magnetocentrifugally driven disk winds  
*(see for example Blandford & Payne 1982)*

# MRI-driven MHD turbulence



# Launching a jet: current models



Sheikhnezami (2012)

Conditions:

- Magnetic flux perpendicular to the disk
- Magnetic diffusion (to oppose accretion)  $\Rightarrow \alpha_M \sim 1$  (turbulence)
- Strong B-field:  $\beta \sim 1$

Based on Blandford & Payne (1982)





## JETS

*Requires strong vertical field  
(Blandford & Payne 1982)*

## DISK WINDS

## MHD TURBULENCE

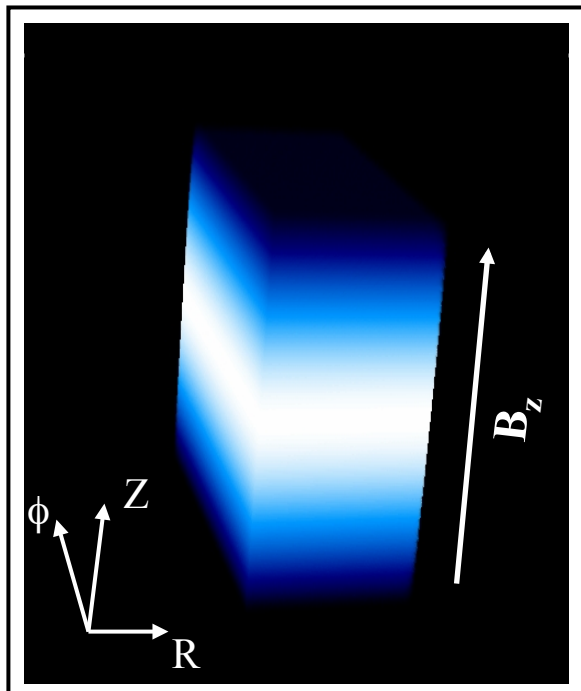
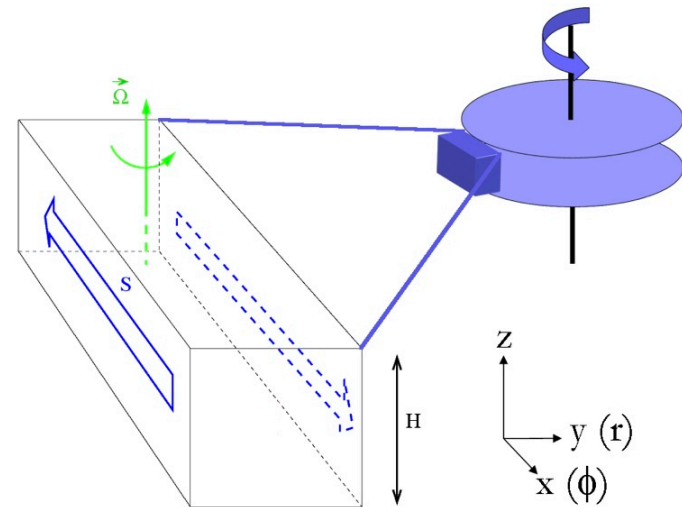
*Weak B-field*

- How do jets/winds/turbulence come to be simultaneously?
- What are the properties of stratified disks when threaded by a B-field?

# **Numerical methods**

# The shearing box model

- 
- **Local approximations**
  - **MHD equations + dissipation (or not)**
  - **Isothermal EQS**
- 



- 
- **Density stratification in vertical direction**
  - **Magnetic field**
    - ✓ Purely vertical, uniform
    - ✓  $\beta = P_{\text{th}}/P_{\text{mag}} = 10^4$  and  $10^5$
  - **Boundary conditions: outflow**
- 
- 

## Two codes

- **RAMSES** (*Teyssier 2002, Fromang et al. 2006*)
  - **PLUTO** (*Mignone et al. 2007*)
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# **Local outflows from turbulent discs**

Fromang, Latter, Lesur & Ogilvie, 2013, A&A

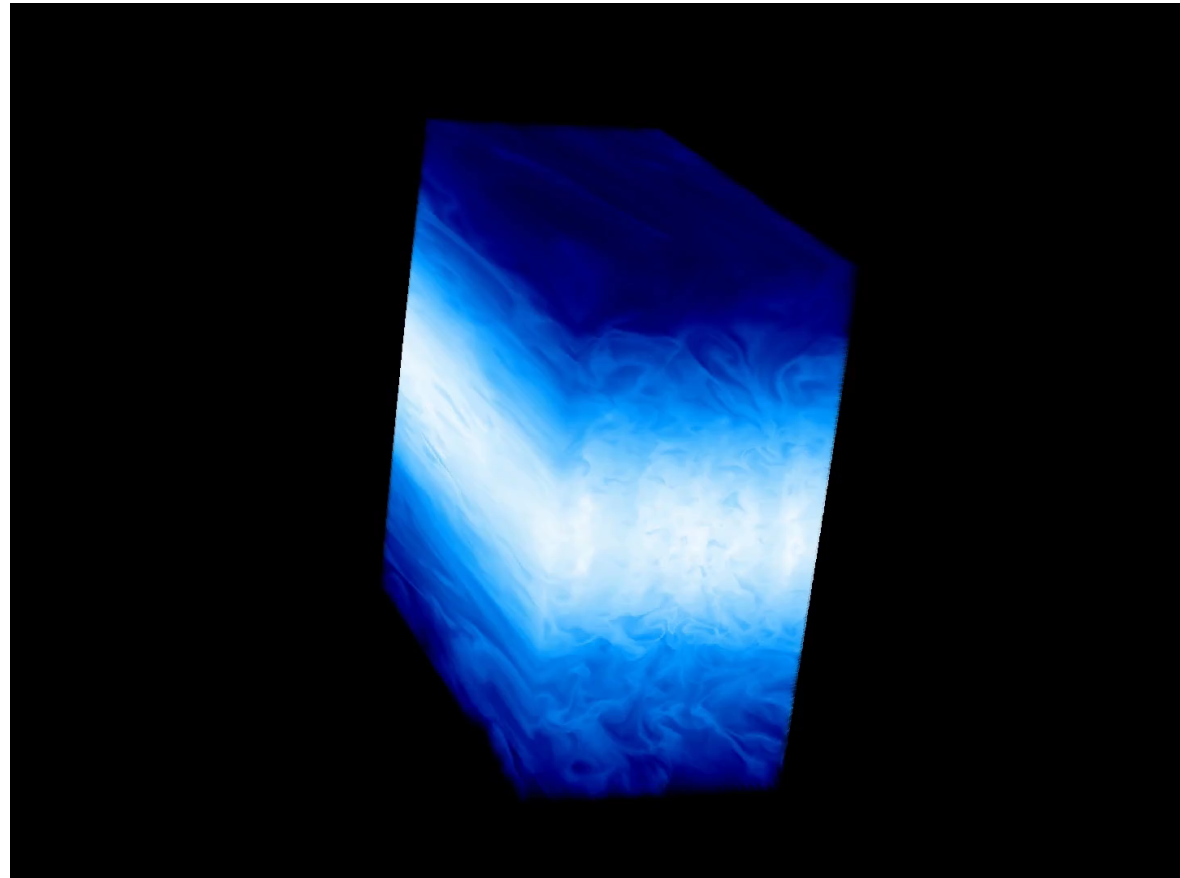
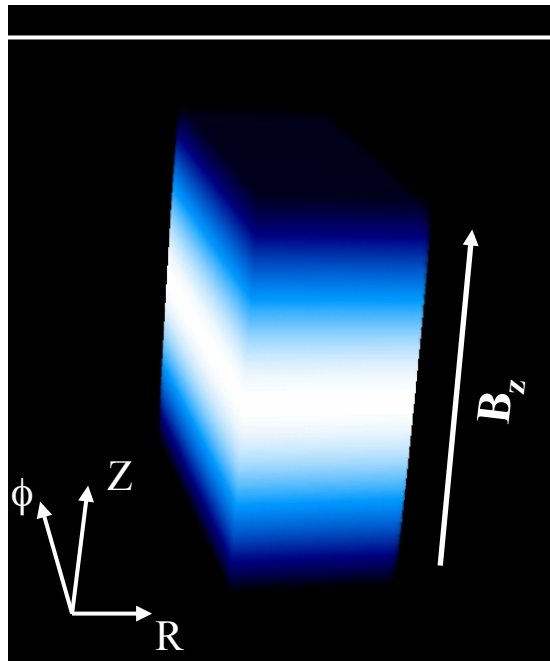
# General flow properties

## Movie:

B.Thooris (CEA/Saclay)

D.Pomarede (CEA/Saclay)

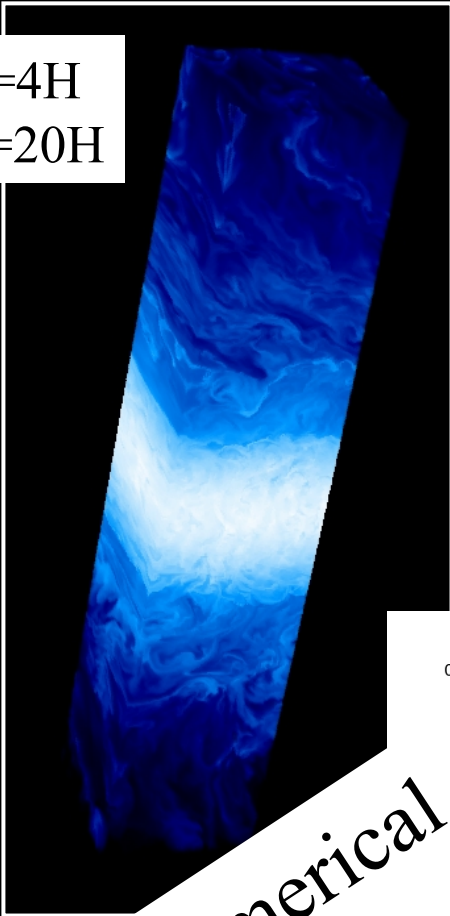
Software: SDvision



Typical turbulent flow in the equatorial plane  
 $\alpha \approx 10^{-2}$   
Powerful outflow launched through the surfaces

# Outflows: effect of the box size

$L_x=4H$   
 $L_z=20H$

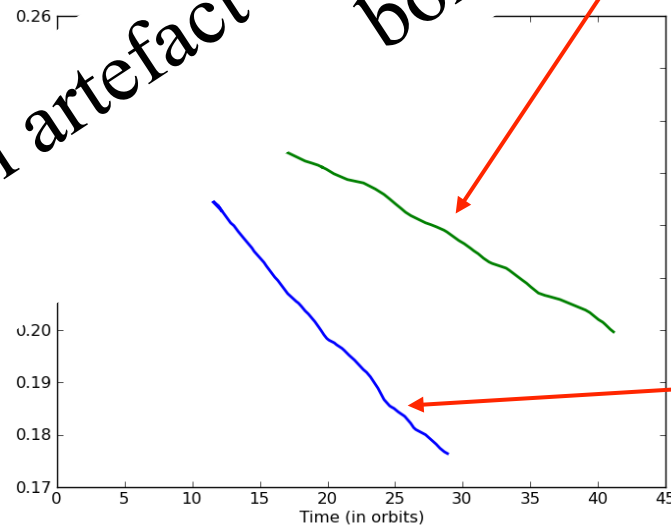


- 64 cells/H
- $L_y=4H$
- $Re=Rm=3000$
- $\beta=10^4$

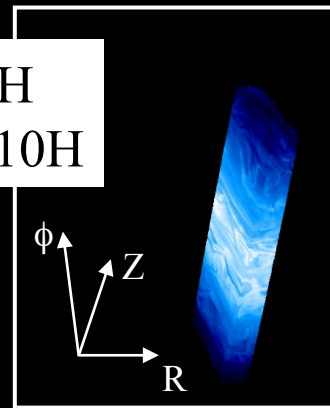
$L_x=4H$   
 $L_z=10H$



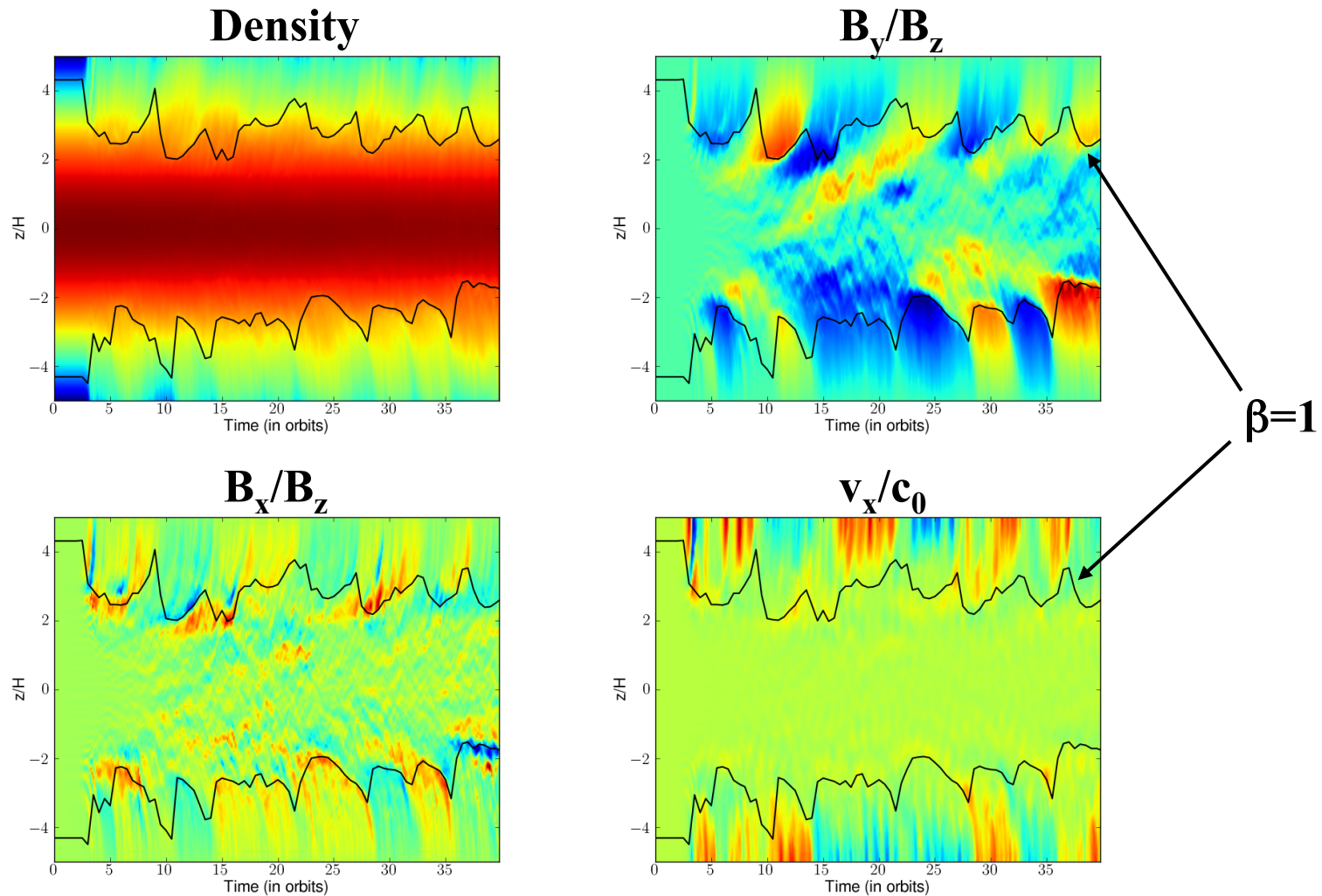
Numerical artefact associated with the shearing box?



$L_x=H$   
 $L_z=10H$



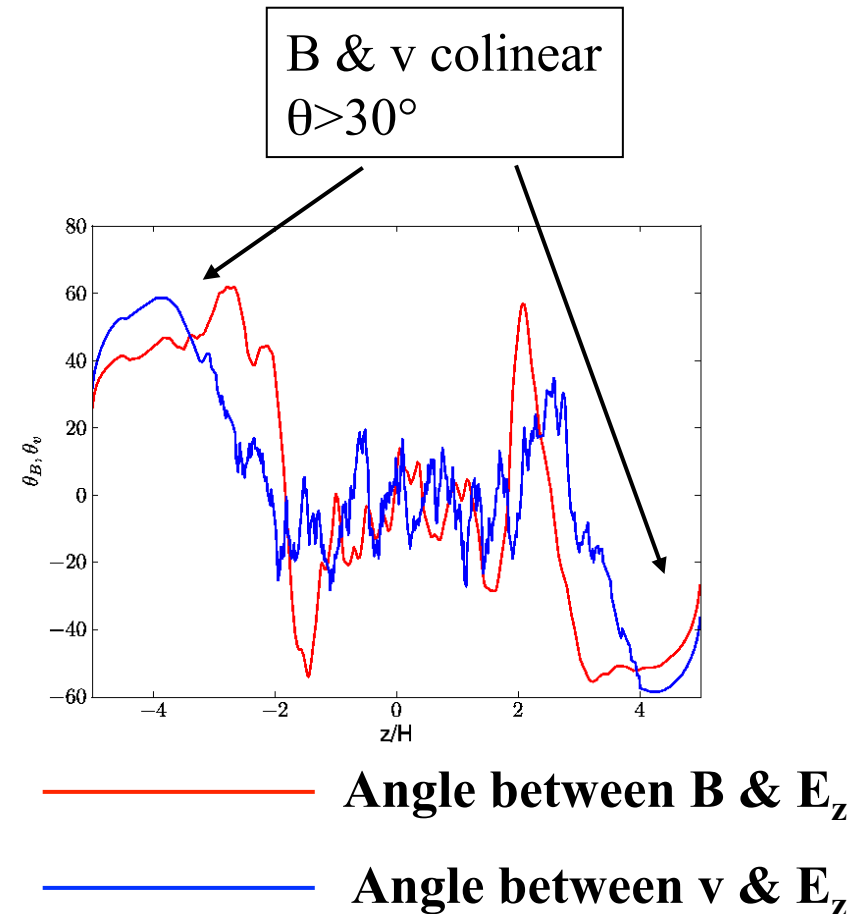
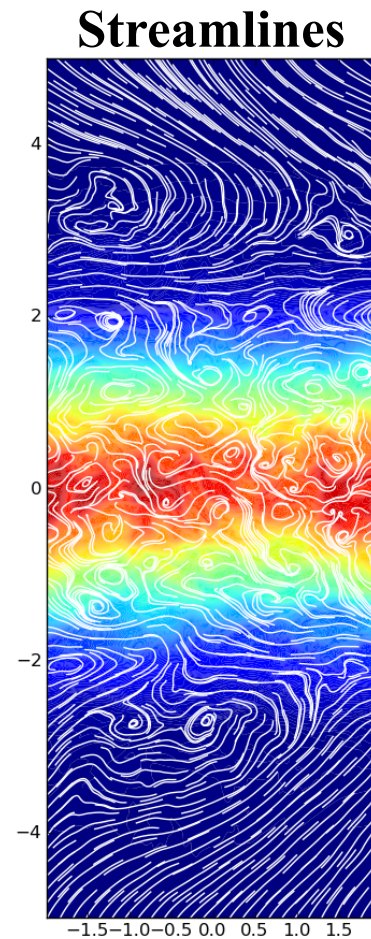
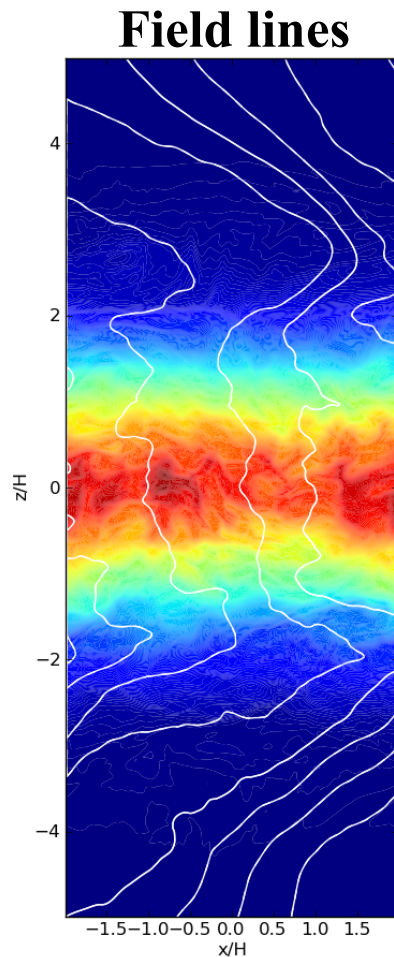
# Outflow structure: spacetime diagram



- $\Rightarrow$  **Bursty ejection: cycles with period of a few orbits**
- $\Rightarrow$  **« Unphysical » geometry of the wind structure**

# Flow structure during a single burst

- Consider one burst
- Time averaged simulation data (example:  $22 < t < 27$ )



**MAGNETOCENTRIFUGAL LAUNCHING POSSIBLE!**  
(Blandford & Payne 1982)

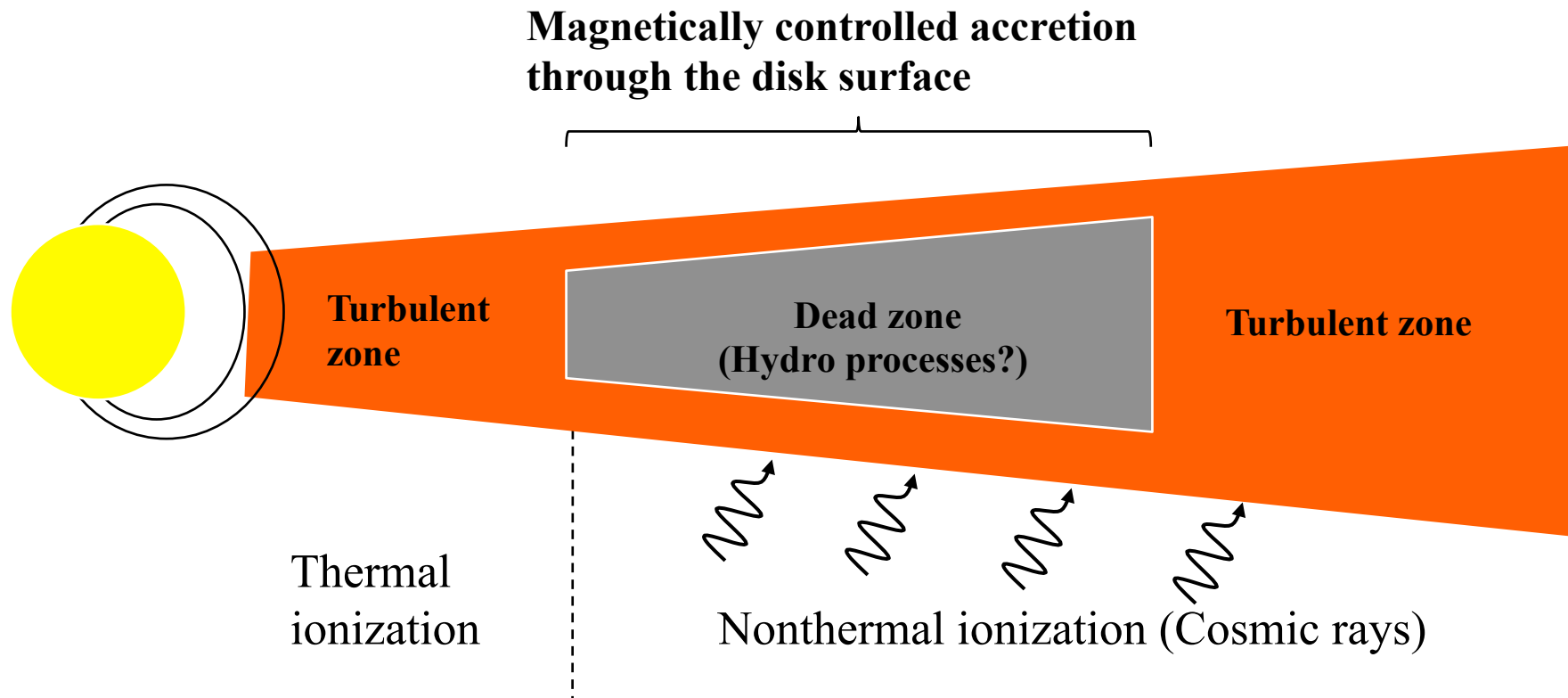
# **The case of protoplanetary discs**

Lesur, Kunz & Fromang, 2014, A&A



# Layered accretion in PP disk

*Gammie (1996)*



## **Pro's of the Dead zone paradigm:**

- tentatively accounts for T-Tauri accretion rates
- provides a « quiet » environment for planet formation
- confirmed by numerical simulations (Fleming & Stone 2003)

## **Con's:**

- only based on an estimate of the Ohmic diffusivity

# Non-ideal MHD: the induction equation

$$\frac{\partial \mathbf{B}}{\partial t} = \nabla \times \left( \mathbf{v} \times \mathbf{B} - \underbrace{\frac{4\pi\eta}{c} \mathbf{J}}_{\text{Ohmic dissipation}} - \underbrace{\frac{4\pi\eta_H}{c} \mathbf{J} \times \hat{\mathbf{B}}}_{\text{Hall effect}} - \underbrace{\frac{4\pi\eta_A}{c} \mathbf{J}_\perp}_{\text{Ambipolar diffusion}} \right)$$

Ohmic  
dissipation

Hall effect

Ambipolar  
diffusion

$$\eta_H \sim \frac{T^{1/2}}{x_e}$$

$$\eta_H \sim \frac{cB}{4\pi en_e}$$

$$\eta_A \sim \frac{B^2}{4\pi\gamma_i\rho_i\rho}$$

$$Rm = \frac{v_A^2}{\eta\Omega}$$

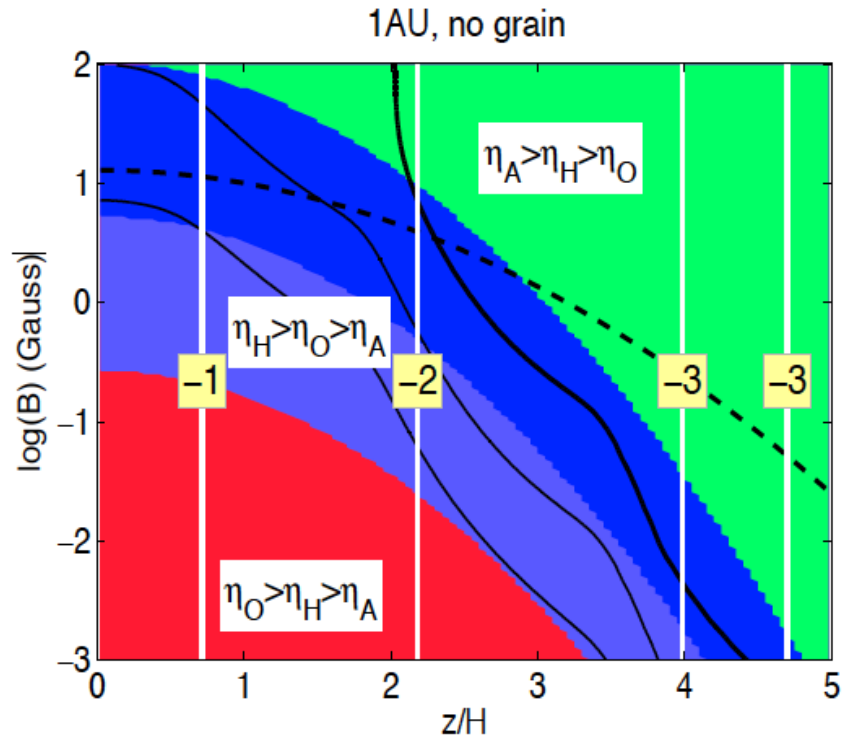
$$\chi = \frac{v_A^2}{\eta_H\Omega}$$

$$Am = \frac{v_A^2}{\eta_A\Omega}$$

Elsasser numbers

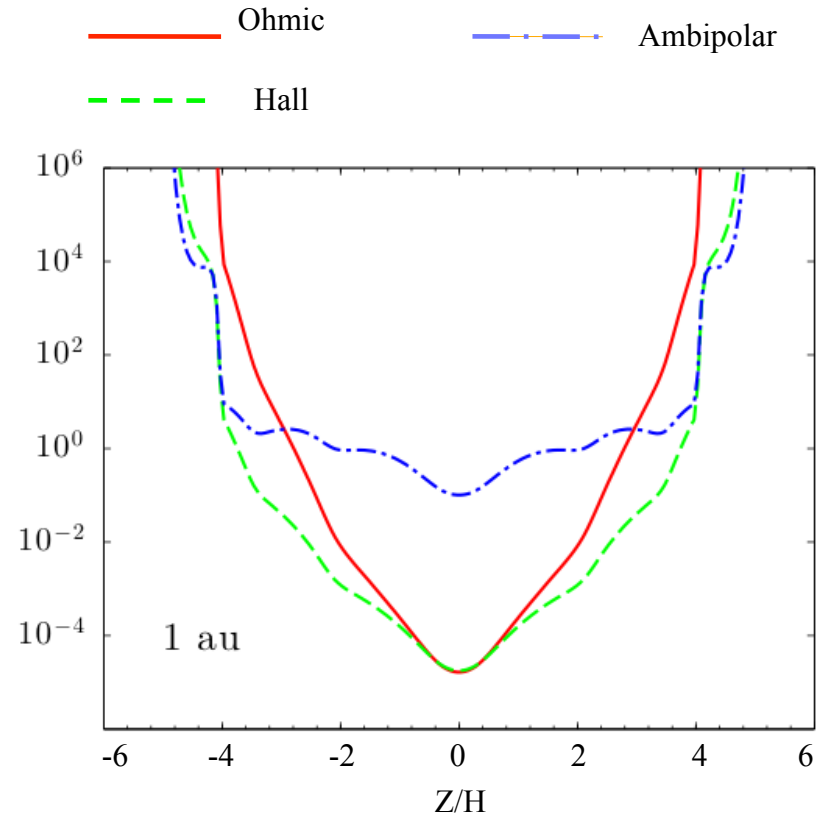
# Non ideal MHD in PP disks?

## Resistivities



*Bai (2011)*

Elsasser numbers @ 1AU

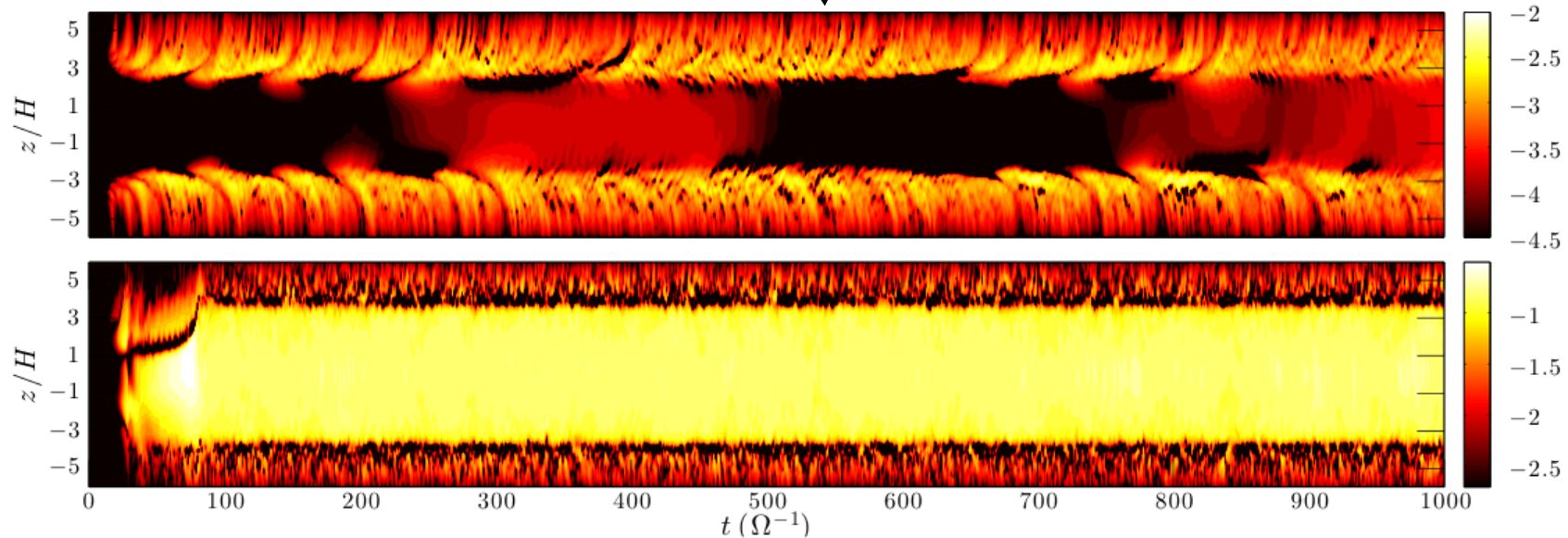


*Lesur et al. (2014)*

Hall term dominant dissipation term in large part of PP disks!

# The effect of the Hall term ( $\beta=10^5$ )

Ohmic dissipation alone @ 1AU  
Stress tensor spacetime diagram:  $\alpha=2.5 \cdot 10^{-3}$



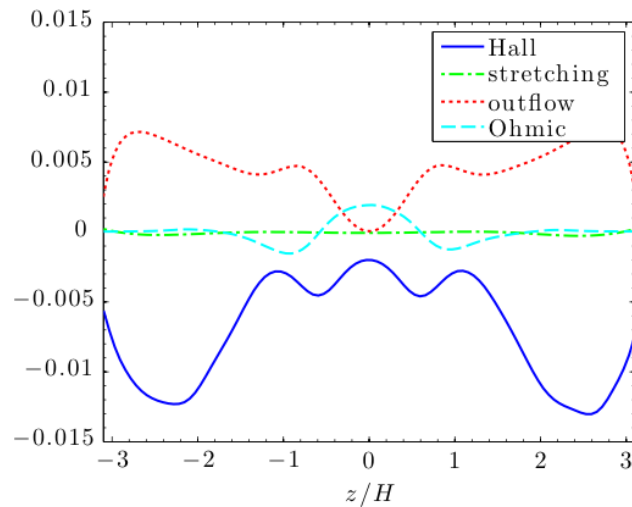
Ohmic dissipation + Hall effect (@ 1 AU)  
Stress tensor spacetime diagram:  $\alpha=4.5 \cdot 10^{-1}$

- Large stress & azimuthal field in the Hall dominated region
- Flow laminar in the disk midplane, powerful outflows

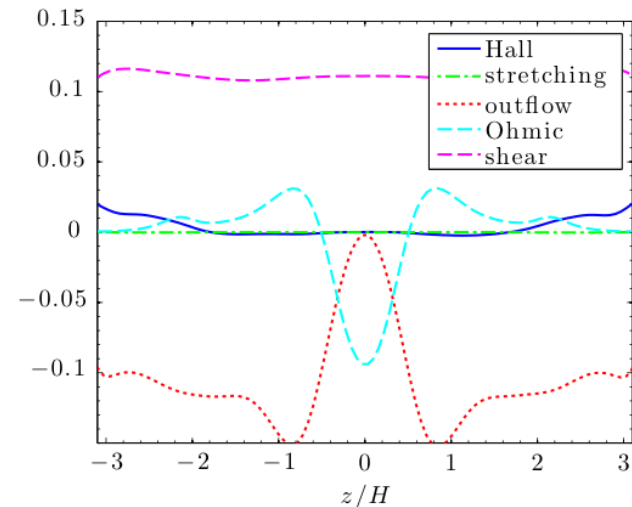
# Physical origin of the midplane stress

Evolution equations

$$\left\{ \begin{aligned} \frac{\partial \langle B_x \rangle}{\partial t} &= \underbrace{\frac{\partial \langle B_x v_z \rangle}{\partial z}}_{\text{Outflow}} - \underbrace{\frac{\partial \langle B_z v_x \rangle}{\partial z}}_{\text{Stretching}} - \underbrace{\frac{\partial}{\partial z} \left( \frac{c}{\sqrt{4\pi en_e}} \frac{\partial \langle B_y \rangle}{\partial z} \right)}_{\text{Hall}} + \underbrace{\frac{\partial}{\partial z} \left( \eta \frac{\partial \langle B_x \rangle}{\partial z} \right)}_{\text{Ohmic}} \\ \frac{\partial \langle B_y \rangle}{\partial t} &= \underbrace{\frac{\partial \langle B_y v_z \rangle}{\partial z}}_{\text{Outflow}} - \underbrace{\frac{\partial \langle B_z v_y \rangle}{\partial z}}_{\text{Stretching}} - \underbrace{\frac{\partial}{\partial z} \left( \frac{c B_0}{\sqrt{4\pi en_e}} \frac{\partial \langle B_x \rangle}{\partial z} \right)}_{\text{Hall}} + \underbrace{\frac{\partial}{\partial z} \left( \eta \frac{\partial \langle B_y \rangle}{\partial z} \right)}_{\text{Ohmic}} - \underbrace{q \Omega \langle B_x \rangle}_{\text{Shear}} \end{aligned} \right.$$



Bx evolution equation



By evolution equation

# Physical origin of the stress

Evolution equations

$$\left[ \begin{array}{l} \frac{\partial \langle B_x \rangle}{\partial t} = \frac{\partial \langle B_x v_z \rangle}{\partial z} \\ \frac{\partial \langle B_y \rangle}{\partial t} = \frac{\partial \langle B_y v_z \rangle}{\partial z} \end{array} \right. - \frac{\partial}{\partial z} \left( \frac{c}{\sqrt{4\pi e n_e}} \frac{\partial \langle B_y \rangle}{\partial z} \right) + \frac{\partial}{\partial z} \left( \eta \frac{\partial \langle B_y \rangle}{\partial z} \right) - q\Omega \langle B_x \rangle$$

Outflow
Hall
Ohmic
Shear

- Hall term creates large negative  $B_x$  (due to large drift velocity of electrons)
  - balanced by outflow
- Shear flow creates large  $B_y$  out of  $B_x$ 
  - balanced by ohmic dissipation (midplane) and outflow (upper layers)

Hall-shear instability (*Kunz 2008*) balanced by Ohmic dissipation and outflows

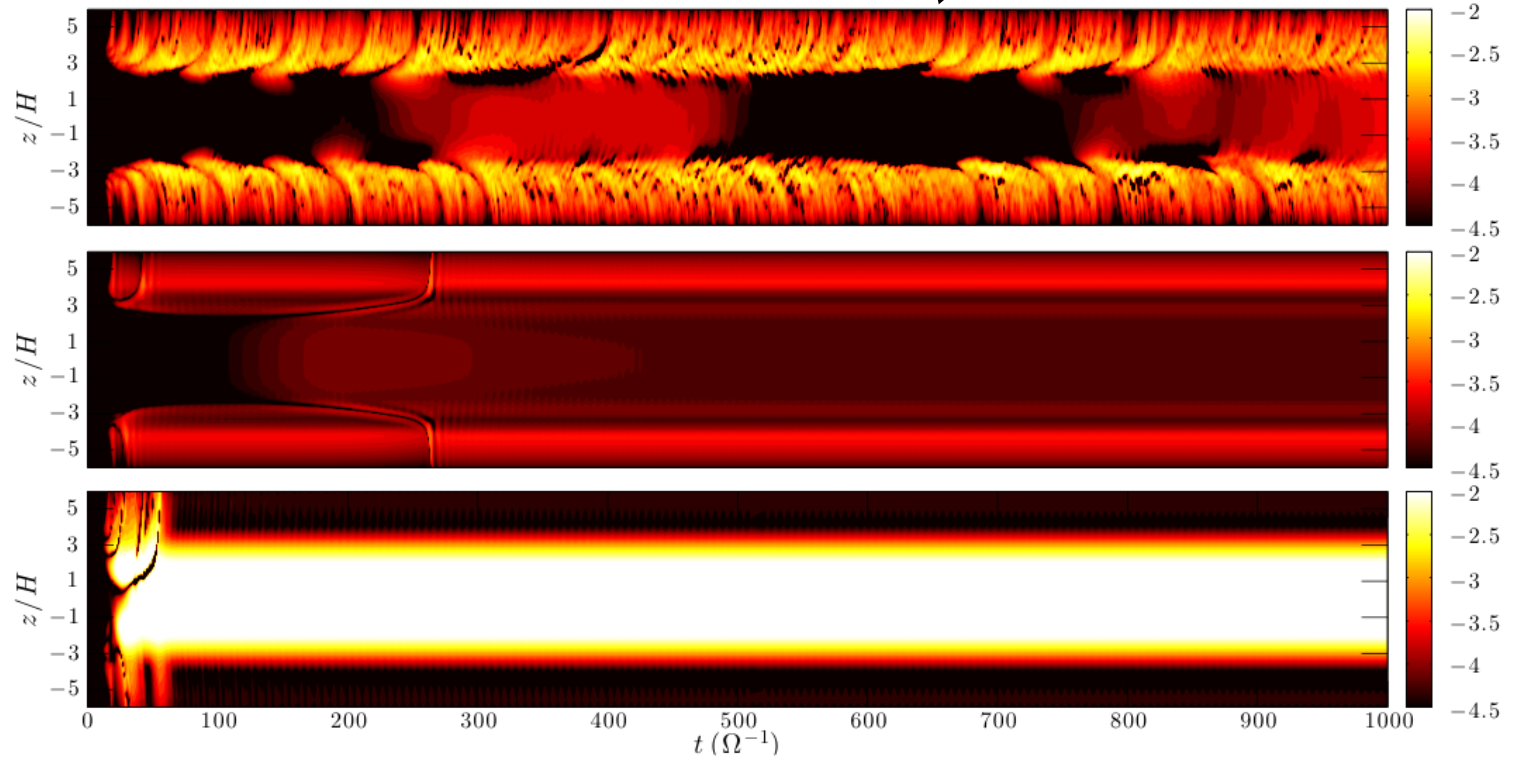
**LARGE STRESS IN HALL DOMINATED REGION**



# Putting things together (Ohm+Hall+Ambipolar)

Ohmic + Ambipolar (1AU)  
 $\alpha=5.9 \cdot 10^{-4}$

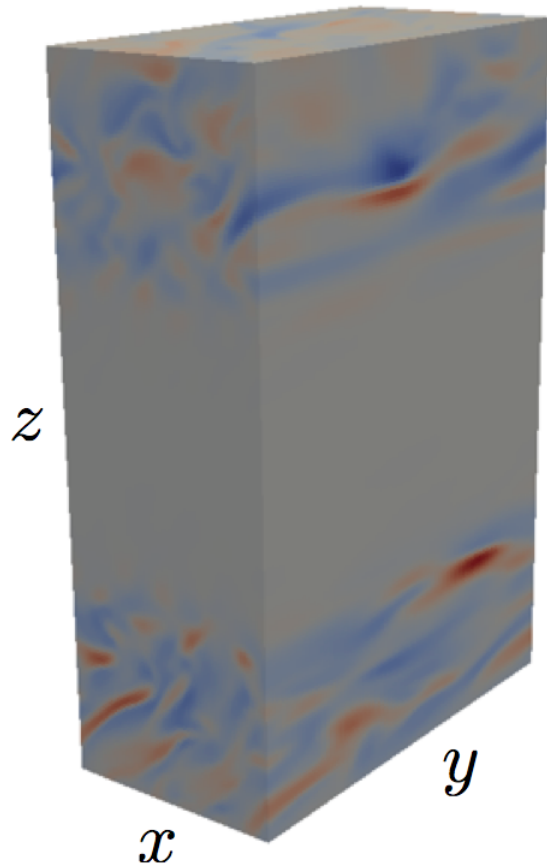
Ohmic dissipation alone (1AU)  
 $\alpha=2.5 \cdot 10^{-3}$



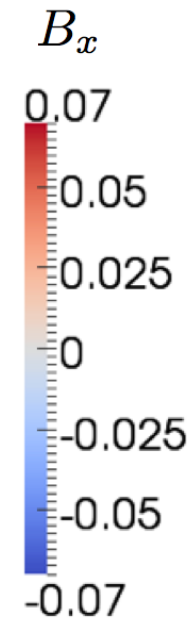
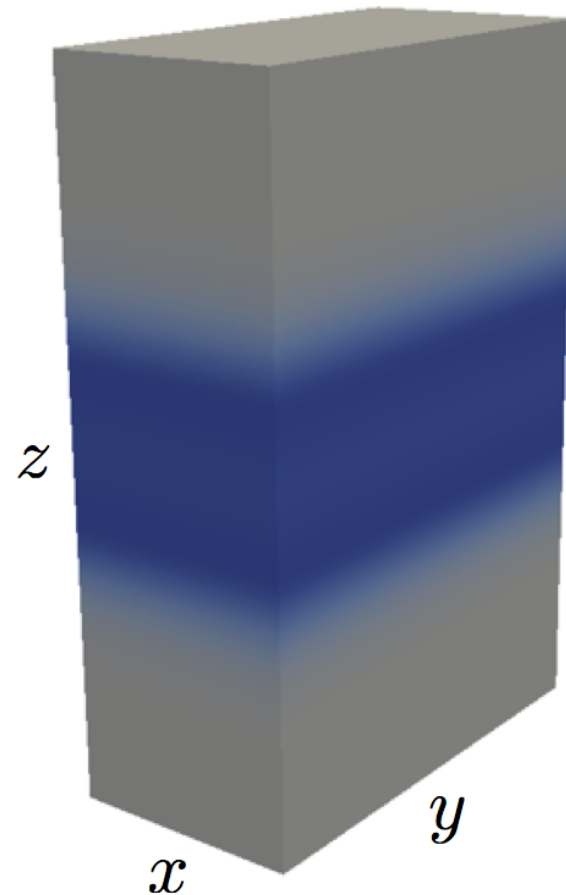
Ohmic + Ambipolar + Hall(1AU)  
 $\alpha=5.0 \cdot 10^{-2}$

# Transport not due to turbulence

Ohmic only  
(« layered accretion »)



Ohmic+AD+Hall

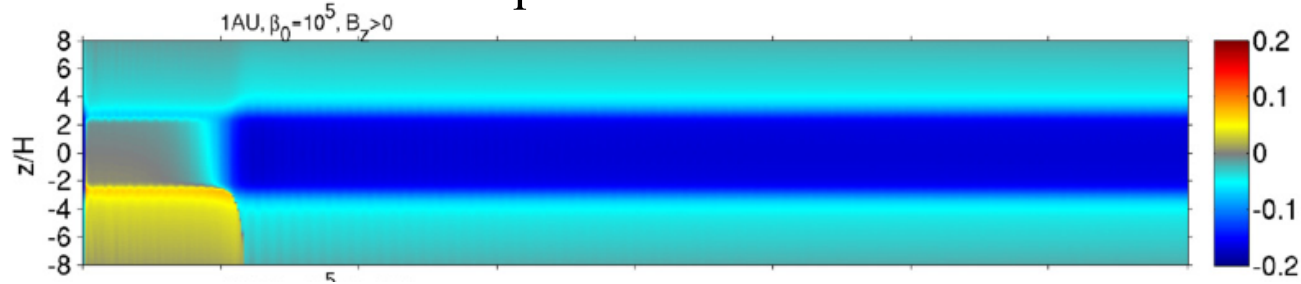


Locality of angular momentum transport?

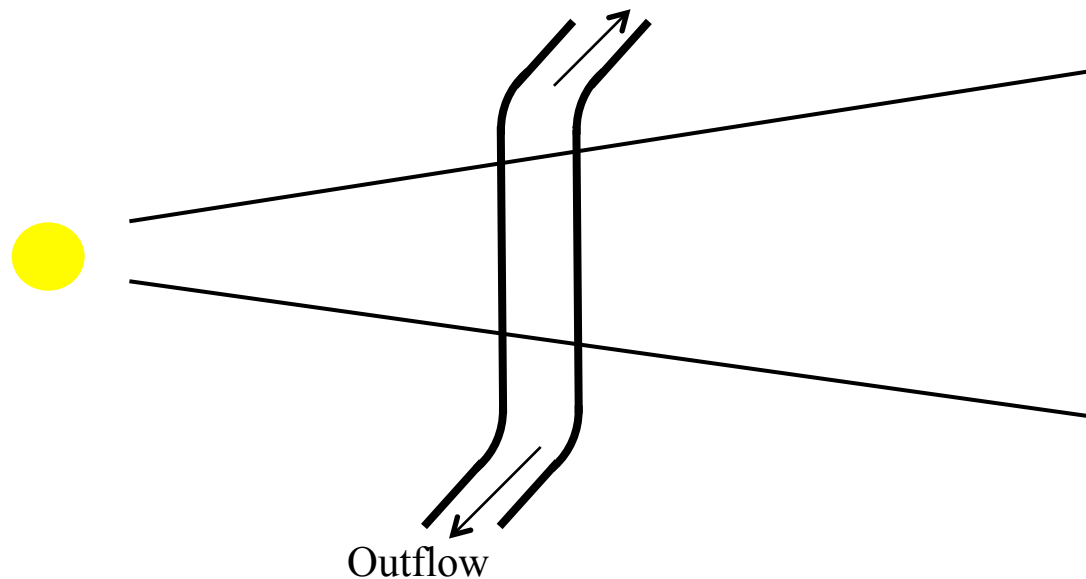
*Balbus & Papaloizou (1999)*

# Current status & problems

Results confirmed by Bai & Stone (2014) using 1D simulations performed with Athena...



...but issues remains associated with the symmetry of the solution



# Conclusions

- **MRI in shearing box simulations drives a strong wind when a vertical field is present**
- **Typical B&P type of solutions seem to coexist with MRI-driven turbulence**

- 
- **Hall term changes the flow properties**
  - **Laminar midplane region, yet strong torque**

- 
- **Numerical artefact(s) seem(s) to affect the simulation**
    - ⇒ **Quantitative estimate of wind properties unreliable...**
    - ⇒ **Global simulations required**